Final Project Report

GRID-AWARE ROBUST FAST-CHARGING STATION DEPLOYMENT FOR ELECTRIC BUSES UNDER SOCIOECONOMIC CONSIDERATIONS

Prepared for Teaching Old Models New Tricks (TOMNET) Transportation Center





Georgia Tech





By

Xinyi Zhao¹ Email: <u>xyzhao24@uw.edu</u>

Chaoyue Zhao¹ Email: <u>cyzhao@uw.edu</u>

Grace Jia² Email: <u>gracejia@uw.edu</u>

¹Department of Industrial & Systems Engineering University of Washington Seattle, WA 98195

²THINK lab (<u>https://sites.uw.edu/thinklab</u>) University of Washington Seattle, WA 98195

October 2023

TECHNICAL REPORT DOCUMENTATION PAGE

1 D (N					
1. Report No.	2. Government Accession No.	3. Recipient's Catalog No.			
N/A	N/A	N/A			
4. Title and Subtitle	5. Report Date				
Grid-aware robust fast-charging station	10/31/2023				
under socioeconomic considerations		6. Performing Organization Code			
		N/A			
7. Author(s)		8. Performing Organization Report No.			
Xinyi Zhao, https://orcid.org/0000-000	02-9655-4889	N/A			
Chaoyue Zhao, https://orcid.org/0000-	0003-0442-2991				
Grace Jia, https://orcid.org/0000-0003	-3894-8924				
9. Performing Organization Name a	nd Address	10. Work Unit No. (TRAIS)			
Industrial and Systems Engineering,		N/A			
University of Washington,		11. Contract or Grant No.			
1410 NE Campus Pkwy, Seattle, WA	98195				
12. Sponsoring Agency Name and A	ddress	13. Type of Report and Period Covered			
U.S. Department of Transportation,		Research Report			
University Transportation Centers Pro	gram,	(11/1/2022 - 10/31/2023)			
1200 New Jersey Ave, SE, Washingto	n, DC 20590	14. Sponsoring Agency Code			
		USDOT OST-R			
15. Supplementary Notes					
Codes on the GitHub repository: https	://github.com/Xinvi-0724/GTFS Tr	ansPowerNet			
Paper: https://arxiv.org/abs/2309.0742	2				
	<u> </u>				
16. Abstract					
The transition from traditional bus flee	ets to zero-emission ones necessitate	s the development of effective planning			
models for battery electric bus (RFR)	charging infrastructure On-route fas	at charging stations distinct from on-base			
charging stations, present unique chall	enges related to safe operation and r	ower supply capacity making it difficult to			
charging stations, present unique chall	enges related to safe operation and p	ower supply capacity, making it difficult to			

models for battery electric bus (BEB) charging infrastructure. On-route fast charging stations, distinct from on-base charging stations, present unique challenges related to safe operation and power supply capacity, making it difficult to control grid operational costs. This paper establishes a novel framework that integrates the bus route network and power network, which leverages the inter-dependency between both networks to optimize the planning outcomes of on-route BEB charging stations in South King County. The problem is formulated as a mixed-integer second-order cone programming model, aiming to minimize the overall planning cost, which includes investments in charging equipment, power facility, and grid operation. Furthermore, fairness measurements are incorporated into the planning process, allowing for the consideration of both horizontal transit equity and vertical transit equity based on different zone merging criteria within the county's existing census tracts. The results of this planning model offer valuable insights into achieving both economic efficiency and social justice in the design of on-route charging facilities for BEBs in South King County.

17. Key Words	18. Distribution Statement		
Battery electric bus, Coupled network	No restrictions.		
programming, Fairness measurement			
19. Security Classif.(of this report)	20. Security Classif.(of this page)	21. No. of Pages	22. Price
Unclassified	31	N/A	
Form DOT F 1700.7 (8-72)	F	Reproduction of complete	ed page authorized

DISCLAIMER

The contents of this report reflect the views of the authors, who are responsible for the facts and the accuracy of the information presented herein. This document is disseminated in the interest of information exchange. The report is funded, partially or entirely, by a grant from the U.S. Department of Transportation's University Transportation Centers Program. However, the U.S. Government assumes no liability for the contents or use thereof.

ACKNOWLEDGMENTS

This study was funded by a grant from A USDOT Tier 1 University Transportation Center, supported by USDOT through the University Transportation Centers program. The authors would like to thank the TOMNET and USDOT for their support of university-based research in transportation, and especially for the funding provided in support of this project. The authors would like to extend their special thanks to Dr. Cynthia Chen, Professor at the University of Washington, for her invaluable suggestions throughout this research project.

TABLE OF CONTENTS

TEC	HNICAL	REPORT DOCUMENTATION PAGE
DIS	CLAIME	3
ACK	KNOWLE	DGMENTS
EXE	CUTIVE	SUMMARY
1.	Introduct	ion7
2.	Literature	e Review
	2.1	Power Grid Interaction
	2.2	Transit Equity
3.	Data Col	lection
4.	Model Fo	prmulation
	4.1	Objective Function
	4.2	Constraints
	4.3	Model Relaxation
5.	Fairness 1	Measures
6.	Planning	Results
	6.1	Planning Results without Fairness
	6.2	Planning Results with Fairness Consideration
7.	Conclusio	ons and Policy Implications
REF	ERENCE	S

LIST OF TABLES

Table 1 Geographically Overlapping Nodes between the Transportation Network and the
Distribution Power Network
Table 2 On-Route Charging Frequency per Round-Trip for Each Bus Route at Different
Departure SOC
Table 3 Summary of Planning Results without Fairness Consideration When Initial SOC Ranges
from 0.1 to 0.4
Table 4 Summary of Planning Results Considering Horizontal Equity with a Maximum Number
of BEB Routes Imax = 5
Table 5 Summary of Planning Results Considering Vertical Equity with a Maximum Number of
BEB Routes Imax = 5

LIST OF FIGURES

Figure 1 Map of air pollution vulnerable areas and priority quintiles for zero-emission bus	
service in King County	. 11
Figure 2 Representation of network topology for the 24-node distribution power network	. 12
Figure 3 Representation of network topology for the 84-Node transportation network	. 12
Figure 4 Optimal placement and charging pile allocation result of charging stations without	
fairness consideration	. 22
Figure 5 Planning results reflecting the highest level of horizontal equity across 4 subareas	. 24
Figure 6 Planning results reflecting the highest level of vertical equity across 3 subareas	. 26

EXECUTIVE SUMMARY

This paper presents a novel mixed-integer second-order cone programming (MISOCP) model that aims to optimize the placement of BEB on-route charging infrastructure. The objective is to minimize the planning and operation costs associated with the fleet electrification process in South King County, considering both the transportation and power systems. Additionally, we emphasize the importance of equity in the planning stage by incorporating fairness measurements, ensuring both horizontal and vertical equity. This research makes two primary contributions:

- 1) To address the potential challenge of BEB charging infrastructure on the power system effectively, we have implemented a coupled networks approach that integrates the local power grid and the bus networks into our planning model. Using South King County as a representative example, our proposed generic framework focuses on establishing a virtual power grid based on the under-planning bus network. By strategically deploying on-route charging stations at bus stops via solving the planning model, we establish coupling relationships between transportation nodes and power grid nodes, effectively integrating the two systems in the planning outcome.
- 2) To ensure equity in fleet electrification, we incorporate Jain's index as a fairness metric in our planning model for BEB charging infrastructure. In South King County, we aggregate census tracts based on both population and bus-commuter features, creating distinct subareas. By imposing a fairness constraint that ensures the desired level of Jain's index in these subareas, we promote equity in the planning results. The planning outcomes in the population-based subareas exhibit horizontal equity, ensuring an equal distribution of resources among all individuals. Conversely, the planning outcomes in the bus-commuter-based subareas demonstrate vertical equity, aiming for a fair allocation within the bus-commuter group.

1. Introduction

With a 27% contribution to greenhouse gas emissions in 2020, the transportation system is the biggest economic sector that consumes fossil fuels [1]. To reduce the exhaust gas emissions of public transportation, the concept of electromobility, involving the adoption of electric vehicles (EVs) for transportation purposes, is rapidly being embraced by public transportation authorities. When it comes to bus systems, electromobility offers substantial advantages in terms of decreased operating and maintenance costs, increased energy efficiency, improved reliability, and reduced air and noise pollution [2].

Over recent decades, the global implementation of bus fleet electrification has emerged as a prominent and noteworthy trend. Notably, Shenzhen in China became the world's first city to fully electrify its public transit bus fleet in 2018, marking a historic achievement [3]. In Europe, the nations of the Netherlands and Luxembourg have made notable strides, with more than half of their registered city buses categorized as zero-emission vehicles [4]. Similarly, King County in Washington, USA, has positioned itself as an early adopter of electric buses and is ambitiously transitioning towards a completely zero-emissions fleet by 2035 [5]. With remarkable advancements in battery technology, battery electric buses (BEBs) are becoming increasingly viable and appealing options for sustainable urban mobility, thus propelling cities worldwide toward a cleaner and more environmentally friendly future.

As bus agencies embrace this transition, they are driven by the dual objectives of ensuring economic efficiency and maintaining the service quality of their BEB fleets. Consequently, the optimization of charging infrastructure planning in this area becomes crucial, aiming to minimize investment and operation costs associated with the required charging facilities [6] as well as any additional costs that may arise during the electrification process.

2. Literature Review

A significant body of literature suggests that bus agencies often opt to construct charging facilities at designated base stations. In this approach, electric buses can only be charged after completing one or multiple full trips [7][8], requiring them to deviate from their scheduled routes [9] and travel deadheading distances for the purpose of charging [10][11]This off-route charging strategy is typically employed during overnight and layover periods when buses are not in service and have sufficient time for complete battery recharge [12]. However, relying solely on this strategy may prove insufficient, especially in the case of King County, where the current on-base charging facilities can only meet 70% of the bus assignments [13].

To bridge this energy gap, an alternative and promising direction to explore is the implementation of on-route charging stations. By strategically incorporating fast-charging facilities at on-street bus stops [14][15], BEBs can conveniently recharge during regular service operations. However, deploying on-route charging stations presents critical challenges that require attention. From an operational standpoint, limited research in BEB planning has explored the impact of the additional power load imposed by these on-route charging stations on the power grid [16]. This includes assessing power loss costs that may occur during electricity transmission. Furthermore, from a social perspective, the introduction of on-route charging stations must be approached with fairness in mind. Given that these stations can serve specific fixed routes [17], it becomes imperative to ensure an equitable distribution of BEB routes across the regional transportation network. This ensures that diverse communities can access the associated benefits, such as cleaner air and enhanced environmental sustainability offered by BEBs.

Our proposed on-route fast-charging planning method effectively addresses the dual research gaps previously identified. Firstly, we prioritize the impacts on the local power grid in the placement of the on-route fast-charging infrastructure. To achieve this, we have developed a coupled power and transportation network specific to South King County. This integrated approach facilitates optimized planning, minimizing charging infrastructure investment and power system operational costs. Secondly, we recognize the limited attention given to equity in fleet electrification planning within the existing literature. To fill this gap, we have incorporated fairness measures into our planning approach to promote transit equity. Specifically, during the partial implementation of BEB routes in a particular region, our planning method promotes both horizontal and vertical transit equity by carefully selecting routes to be designated as BEB routes from the overall bus network.

The integration of the power and transportation networks, along with considerations of cost optimization and transit equity, positions our approach as an effective and comprehensive solution for the planning of on-route fast charging for BEBs. Furthermore, to emphasize the uniqueness of our method, we thoroughly examine existing research in fleet electrification planning, specifically focusing on the domains of power grid interaction and transit equity.

2.1 Power Grid Interaction

The successful implementation of fleet electrification necessitates a strong interconnection between transportation and power systems. To ensure efficient management of this interaction, an integrated approach that considers the coupled power and transportation network is crucial in charging infrastructure planning. While this approach has received limited attention in the context of electric bus on-route charging stations, some research has integrated the power grid and transportation network when planning EV charging stations. This integration can take two forms: coupling a transportation test case with a power system test case or coupling a real-world transportation network with a power system test case. The latter approach incorporates authentic data and conditions from a functioning transportation system, resulting in enhanced practicality.

In the first type of coupled system, the Sioux Falls network is widely used as a transportation test case. For example, in a study by [18], a coupled network was created using the topology of the Sioux Falls network and a subset of the IEEE-118 bus system. The goal of this study was to allocate a specified number of charging stations for plug-in EVs. The potential locations of these charging stations were identified as common nodes in both the transportation and power grid systems. In another study by [19], the topology of the Sioux Falls network was retained for the transportation system, but the authors used a simplified version of the IEEE 34-bus system for the power grid. The authors matched the destination nodes in the transportation system with the corresponding buses in the power grid, but the intention behind this was unspecified. [20] builts a coupled system using the Sioux Falls network and the IEEE 33-bus system; nevertheless, there was no direct relationship between the road distances and the power line lengths in this study.

In addition to the Sioux Falls network, other researchers have created their own transportation networks to build coupled systems for EV planning. For instance, [21] created a coupled system through the utilization of a nine-node road network and a subset of the IEEE 118-bus system. In this case, each link in the transportation network was connected to a particular bus in the power system, and the energy consumption of EVs on that link resulted in a power load on the grid. [22] employed a 25-node traffic network and an 11 kV 33-node distribution system to construct their coupled system. The authors considered the geographical positioning of the nodes and established a direct relationship between the nodes in the transportation and power systems, where the traffic nodes 1-25 overlapped with the distribution system nodes 1-25. Furthermore, [23] adopted a 25-node highway transportation network and designed a 14-node 110 kV high voltage distribution network to establish a relationship between the transportation link distance and the power line length within their coupled system.

Regarding the second type of coupled system, an exemplar is a work by [9], who employed a real-world transportation network from the city of Shenzhen and integrated it with the virtual power network established by [23]. To retrieve distances within the transportation network, they utilized the API of Baidu Map. However, it is important to note that their studies did not account for the correlation between the actual road distance and the line length in the virtual power network.

Building upon the second type of coupled system discussed in the literature, we propose a comprehensive framework that integrates a real-world transportation network with a virtual power system. Our framework establishes a correlation between the actual bus route distance and

the power line length in the coupled system, enhancing the practicality of the planning outcome. Unlike previous approaches, our framework is designed to be adaptable and suitable for various bus networks in different regions. By utilizing our generic coupled network framework, our objective is to address the existing research gap and provide a comprehensive solution for onroute BEB charging infrastructure planning.

2.2 Transit Equity

Existing research has highlighted the presence of transit inequities among underserved communities, including people of color and low-income individuals, due to inadequate spatial coverage of transportation infrastructure [24][25]. Addressing and rectifying this long-standing spatial gap between low-income settlements and their access to transit services pose great challenges [26]. However, fleet electrification, being a significant transit initiative, presents an opportunity to address these inequities right from the planning phase. This involves strategically locating charging infrastructure and designing efficient routes to serve historically underserved areas [27]. By adopting an equitable perspective, BEB planning [28] can serve as a means to mitigate the discriminatory impact on socially vulnerable populations caused by transit-related spatial mismatch.

The concept of transit equity encompasses two dimensions: horizontal equity, promoting equal treatment for all individuals [29], and vertical equity, tailoring treatments to diverse needs or circumstances [30]. Despite the importance of transit equity, there is a noticeable dearth of research that applies its principles to transportation-network-related planning [31]. [32] were the first to consider horizontal equity in solving the transportation network redesign problem by introducing a spatial equality constraint. Building upon this work, [31] combines both horizontal and vertical equity goals in a constraint of the transit network design problem, ensuring that the final configuration of the public transport service strikes the fairest compromise by considering both spatial distribution and social needs.

Furthermore, in the context of electric bus planning, there is even less research that incorporates transit equity. The work conducted by [33] closely aligns with our research scope. They proposed a bi-objective model to support transit agencies in the optimal deployment of BEBs, taking into account capital investment and environmental equity. However, their primary focus lies in maximizing vertical equity in one of their objectives, which involves weighting disadvantaged populations based on air pollutant concentration. Notably, to the best of our knowledge, there have been no attempts to incorporate both horizontal and vertical equity into the planning problems of electric bus charging infrastructure.

Given the limited research on the topic, it becomes necessary to draw upon metrics used in other domains to measure the fairness of the transit planning result. [31] employed the Gini coefficient, a widely used fairness metric in economics, to develop their equality constraint. Similarly, we have identified Jain's index, which is commonly used to measure fairness in resource allocation within telecommunication networks [34], as a suitable metric to characterize the distribution of BEB routes across a bus network in a given region.

3. Data Collection

Neighborhoods in King County that are burdened with elevated air pollution levels tend to be home to low-income households and marginalized racial and ethnic groups [13]. This disparity is demonstrated in Figure 1, where the southern base areas, encompassing Renton, Burien, Tukwila, SeaTac, and Kent, are prominently affected. These communities have long endured inadequate transportation services, resulting in heightened exposure to transportation-related noise and air pollution. Notably, the South Base exhibits a higher number of daily service miles compared to other bases, indicating a greater extent of service inadequacy. Moreover, approximately 31% of the census blocks along South Base routes are categorized as highly vulnerable to the adverse impacts of air pollution [28].



Figure 1 Map of air pollution vulnerable areas and priority quintiles for zero-emission bus service in King County

In order to construct a transportation network using the electric bus routes in South King County, we refer to Appendix C of the King County Transit report [13] and exclude the non-operational

bus routes. The remaining routes, including 22, 101, 102, 111, 150, 153, 156, 168, 177, 181, 182, 183, 187, 190, and 193, are used to establish the transportation network. This network is derived from the general transit feed specification (GTFS) data [39].

The topology of the 84-node transportation network is illustrated in Figure 3 and the diagram of the 110-kV high voltage distribution network is shown in Figure 2. For the parameters of the distribution network, please refer to [43]. The resistance and reactance of each power line reflect the actual geographical distance between its connecting power nodes. And the coupling relationship between the power and transportation network nodes is summarized in Table 1.



Figure 2 Representation of network topology for the 24-node distribution power network.



Figure 3 Representation of network topology for the 84-Node transportation network.

In our planning problem, we consider two types of coaches for BEBs: 40-ft and 60-ft. The coach type for each bus route is provided in Appendix C of the King County Transit report [13]. We specifically utilize the 40-ft BYD K9M and 60-ft BYD K11M BEB models, which have battery capacities of 313 kWh and 578 kWh, respectively.

The estimated average energy consumption per kilometer for 40-ft and 60-ft buses are 1.99 kWh/mile and 3.74 kWh/mile, as indicated in the sources [45][46]. According to the official published specifications from BYD [47][48], the nominal charging powers for K9M and K11M electric buses are 150 kW and 200 kW, respectively. Moreover, we have set a maximum waiting time of 12 minutes at each station to ensure that BEBs receive timely energy support.

Power Node	Trans Node	Latitude	Longitude	Powe r Node	Trans Node	Latitude	Longitude
1	1	47.6167107	-122.3306	13	39	47.2959099	-122.24944
2	7	47.545311	-122.38711	14	41	47.315258	-122.17787
3	8	47.5168533	-122.3769	15	43	47.4843712	-122.27198
4	10	47.5933418	-122.32896	16	46	47.4468002	-122.17017
5	17	47.3099785	-122.36103	17	49	47.4616432	-122.14659
6	19	47.4798775	-122.20813	18	50	47.3127861	-122.30338
7	20	47.3871994	-122.30184	19	53	47.2948532	-122.38205
8	21	47.3584251	-122.29468	20	55	47.3651619	-122.01903
9	22	47.4379692	-122.32423	21	56	47.358078	-122.14958
10	26	47.4877625	-122.14824	22	57	47.3667755	-122.10149
11	31	47.3848267	-122.2327	23	69	47.5571404	-122.18928
12	37	47.4413147	-122.24831	24	76	47.5722656	-122.32739

Table 1 Geographically Overlapping Nodes between the TransportationNetwork and the Distribution Power Network

4. Model Formulation

In this section, we present the formulation of a mathematical model designed for BEB on-route charging station planning. We delve into the details of incorporating Jain's index as a fairness measure within the planning framework. The model optimization includes determining the optimal placement of charging stations, the number of charging piles at each station, the interconnection between bus stations and power grid nodes, and the current flow through power lines that connect the bus stations to the power grid.

4.1 Objective Function

The total planning cost for the on-route charging infrastructure of BEBs is determined by considering the costs associated with both the transportation network for constructing the facilities and the power grid for integrating the new charging stations. This cost is represented by (1), which consists of four components that are summed together. The first three components pertain to the investment cost for the charging stations, charging piles, and the power lines connecting the charging stations to the power grid. The final component represents the operational cost, which accounts for the energy loss in the power grid integrated with on-route charging stations.

$$\min \sum_{m \in N^T} (f_{s,m} \cdot X_m + f_{c,m} \cdot \beta_m) + \sum_{m \in N^T} \left(\sum_{i \in N^G} c_{i,m} \cdot \Psi_{i,m} \right) + \sum_{\mathcal{E}: (i,j)} T \cdot c_e \cdot \ell_{ij} \cdot r_{ij},$$
(1)

where $f_{s,m}$ and $f_{c,m}$ stand for the unit cost of charging stations and charging piles at bus station m, respectively. The binary decision variable X_m represents the construction of a charging station at bus station m, with $X_m = 1$ signifying its presence. The integer decision variable β_m represents the number of charging piles installed at bus station m. The cost of constructing the power line that connects bus station m to the power grid node i is represented by $c_{i,m}$, which is determined by the geographical distance between the two nodes. The binary decision variable $\Psi_{i,m}$ indicates whether the power line has been established, where $\Psi_{i,m} = 1$ signifies that bus station m has been successfully integrated into power grid node *i*. The power loss time in the planning period is represented by *T*, while the electricity price is c_e . ℓ_{ij} denotes the square of the magnitude of the complex current from node i to j after building charging stations, while r_{ij} represents the resistance of power line (*i*, *j*).

4.2 Constraints

In order for a bus to be charged at bus station m, it is mandatory for a charging station to be constructed at that location:

$$y_{\alpha,m} \le X_m, \,\forall \alpha \in \Omega_\alpha, \forall m \in N^T,$$
(2)

where $y_{\alpha,m}$ is a binary decision variable, and $y_{\alpha,m} = 1$ denotes the bus on route α charges at bus station m. In addition, it is necessary to construct the charging piles at an established charging station, which can be formalized as follows using a Big-M method:

$$0 \le \beta_m \le M \cdot X_m, \,\forall m \in N^T, \tag{3}$$

where M can be considered as the total number of available charging piles to be invested during the planning period.

To avoid any queuing during the limited on-route charging time slots, a practical approach is to assign dedicated charging piles for each bus route at shared stations. This strategy ensures smooth charging operations and minimizes potential disruptions or delays caused by congested charging stations. Therefore, it is necessary to ensure that the number of installed charging piles is no less than the number of bus routes assigned to charge at the station:

$$\sum_{\alpha \in \Omega_{\alpha}} y_{\alpha,m} \le \beta_m , \forall m \in N^T.$$
(4)

In order to establish a functional coupling between the transportation and power network, it is imperative to connect bus stations that are selected for installing charging infrastructure to a power grid node:

$$\sum_{i \in N_G} \Psi_{i,m} = X_m, \forall m \in N^T.$$
(5)

Given the requirement for all BEBs to complete their round trips successfully, we consider the initial SOC of their batteries, deviating from previous studies [14][36] that assume fully-charged batteries at the start. By exploring various levels of initial SOC as BEBs depart from their origin stations, we can determine the corresponding optimal scale of on-route charging facilities. As a result, we can effectively manage the investment in on-route charging facilities and make efficient use of the existing on-base charging stations at the Interim Base. The initial energy of the BEBs at the time of departure from the origin station o_{α} can be quantified as $\theta_0 \cdot u_{\alpha}^{bat}$, where θ_0 represents the initial SOC of the batteries, and u_{α}^{bat} denotes the specific battery capacity of bus route α .

During BEB operation, it is necessary to maintain the battery's SOC within a specific safe range:

$$e_{\alpha,m} \ge \theta^l \cdot u_{\alpha}^{bat}, \quad \forall \alpha \in \Omega_{\alpha}, \forall m \in N^T.$$
(6)

$$e_{\alpha,m} + s_{\alpha,m} \le \theta^u \cdot u_\alpha^{bat}, \quad \forall \alpha \in \Omega_\alpha, \forall m \in N^T.$$
(7)

where θ^l and θ^u are the lower and upper bounds of the battery capacity of BEBs. $e_{\alpha,m}$ and $s_{\alpha,m}$ represent the energy level and the battery's energy supply in BEBs for route α at the station m.

At each bus station, the energy conservation constraint for BEB batteries accounts for the energy consumption during travel between stations m and n:

$$e_{\alpha,n} = e_{\alpha,m} + s_{\alpha,m} - e_{\alpha}^{0} \cdot d_{mn}, \forall \alpha \in \Omega_{\alpha}, \forall (m,n) \in L_{\alpha},$$
(8)

where e_{α}^{0} denotes the average energy consumption of BEBs per unit distance for route α , which depends on the specific BEB model used. The driving distance between stations m and n is represented by d_{mn} . It is worth noting that we consider round-trip routes for each BEB, and the bus must satisfy the energy conservation constraint during the completion of its route in both directions.

All BEBs are required to adhere to the predefined operation schedule and cannot spend excessive time at a charging station. Therefore, the charging energy must not exceed the maximum available energy supply:

$$0 \le s_{\alpha,m} \le P_{\alpha}^{e} \cdot \tau_{\alpha,m} \cdot y_{\alpha,m}, \forall \alpha \in \Omega_{\alpha}, \forall m \in N^{T},$$
(9)

where P^e_{α} denotes the nominal power of the charging pile for bus route α , and $\tau_{\alpha,m}$ represents the maximum dwelling time for bus route α at station m.

To determine the actual power loss in the power grid after incorporating on-route charging stations, we can utilize a branch flow model as described in [37]:

$$s_j = \sum_{k:j \to k} S_{jk} - \sum_{i:i \to j} (S_{ij} - z_{ij}\ell_{ij}), \forall (i,j) \in \mathcal{E},$$
(10)

$$v_j = v_i - 2(r_{ij}P_{ij} + x_{ij}Q_{ij}) + (r_{ij}^2 + x_{ij}^2) \cdot \ell_{ij}, \forall (i,j) \in \mathcal{E},$$
(11)

$$\ell_{ij} = \frac{P_{ij}^2 + Q_{ij}^2}{\nu_i}, \forall (i,j) \in \mathcal{E},$$
(12)

where s_j represents the power injection at power grid node *j*. S_{ij} denotes the sending-end power flow from node *i* to *j*, given by $S_{ij} = P_{ij} + iQ_{ij}$. z_{ij} is the impedance of line (i, j), represented as $z_{ij} = r_{ij} + ix_{ij}$. ℓ_{ij} represents the square of the magnitude of the complex current from node i to j, while v_j represents the square of the magnitude of the complex voltage at node j. The resistance and reactance of line (i, j) are represented by r_{ij} and x_{ij} , respectively. Furthermore, the real power flow from node i to node j is denoted as P_{ij} , and Q_{ij} signifies the reactive power flow between these nodes.

The power injection at a power grid node in (10) consists of two components: the charging power from integrated on-route charging stations, if applicable, and the original load demand:

$$s_{i} = -\sum_{m \in N^{T}} \sum_{\alpha \in \Omega_{\alpha}} P_{\alpha}^{e} \cdot y_{\alpha,m} \cdot \Psi_{i,m} - s_{i}^{load}, \forall i \in N^{G},$$
(13)

where s_i^{load} is the original load demand of power node i.

For the reliable and safe operation of the power grid after integrating on-route charging stations, it is crucial to maintain both the voltage and current within a specific range:

$$v_i \le v_i \le \overline{v_i}, \,\forall i \in N^G, \tag{14}$$

$$0 \le \ell_{ij} \le \overline{\ell_{ij}}, \forall (i,j) \in \mathcal{E},$$
(15)

where $\underline{v_i}$ and $\overline{v_i}$ denote the lower and upper bound of the square of the node voltage, respectively. $\overline{\ell_{ij}}$ represents the maximum square of the current in line (i, j).

Finally, we ensure that all binary and integer decision variables used in the planning model satisfy the following conditions:

$$X_m \in \{0,1\}, \,\forall m \in N^T,\tag{16}$$

$$\beta_m \in \mathbb{Z}, \, \forall m \in N^T, \tag{17}$$

$$y_{\alpha,m} \in \{0,1\}, \, \forall \alpha \in \Omega_{\alpha}, \forall m \in N^T,$$
(18)

$$\Psi_{i,m} \in \{0,1\}, \,\forall i \in \mathbb{N}^G, \forall m \in \mathbb{N}^T.$$
(19)

4.3 Model Relaxation

In order to make the planning model compatible with commercial solvers like Gurobi and CPLEX, certain nonlinear constraints need to be relaxed. The first constraint to be handled with is (12) due to its quadratic term. To address this, we adopt the approach proposed by [37] and reformulate it as the following second-order cone constraint:

$$\left\| \begin{array}{c} 2P_{ij} \\ 2Q_{ij} \\ \ell_{ij} - \nu_i \end{array} \right\|_2 \leq \ell_{ij} + \nu_i, \, \forall (i,j) \in \mathcal{E}.$$

$$(20)$$

Another non-linearity lies in (13), which involves the product of two binary decision variables $y_{\alpha,m}$ and $\Psi_{i,m}$. We introduce an auxiliary variable $Y_{\alpha,m,i}$ to replace the product. Constraint (13) is then reformulated as follows:

$$s_i = -\sum_{m \in N^T} \sum_{\alpha \in \Omega_{\alpha}} P^e_{\alpha} \cdot Y_{\alpha,m,i} - s^{load}_i, \ \forall i \in N^G.$$

$$(21)$$

To ensure the consistency between the auxiliary variable $Y_{\alpha,m,i}$ and the product of $y_{\alpha,m}$ and $\Psi_{i,m}$, we introduce additional constraints:

$$Y_{\alpha,m,i} \le y_{\alpha,m}, \forall \alpha \in \Omega_{\alpha}, \forall m \in N^T, \forall i \in N^G,$$
(22)

$$Y_{\alpha,m,i} \le \Psi_{i,m}, \, \forall \alpha \in \Omega_{\alpha}, \forall m \in N^T, \forall i \in N^G,$$
(23)

$$Y_{\alpha,m,i} \ge y_{\alpha,m} + \Psi_{i,m} - 1, \, \forall \alpha \in \Omega_{\alpha}, \, \forall m \in N^T, \, \forall i \in N^G,$$
(24)

$$Y_{\alpha,m,i} \in \{0,1\}, \,\forall \alpha \in \Omega_{\alpha}, \forall m \in N^T, \forall i \in N^G.$$

$$(25)$$

Consequently, the entire planning model is reformulated as a MISOCP problem:

$$\min \sum_{m \in N^{T}} (f_{s,m} \cdot X_{m} + f_{c,m} \cdot \beta_{m}) + \sum_{m \in N^{T}} \sum_{i \in N^{G}} c_{i,m} \cdot \Psi_{i,m} + \sum_{\mathcal{E}:(i,j)} T \cdot c_{e} \cdot \ell_{ij} \cdot r_{ij}$$
s.t. (2) - (11), (14) - (25). (26)

5. Fairness Measures

In our model, we utilize Jain's index [38] as a measure of fairness in the planning of on-route charging stations for BEBs. Jain's index possesses several desirable properties, including population size independence, scale and metric independence, boundedness, and continuity. If we divide the planning area in South King County into H areas and assign an allocation of w_h to the hth area, then the expression for Jain's index can be given as follows:

$$f(w) = \frac{(\sum_{h=1}^{H} w_h)^2}{H \sum_{h=1}^{H} w_h^2}$$
(27)

To determine the fairness index w_h in our planning model, we must consider the impact of a zero-emission fleet on the residents of King County. A viable approach to establishing such a fairness index would be to consider the proportion of BEB routes within a specific area relative to all bus routes. To explicitly express the fairness index as a percentage of BEB routes in our planning model, we introduce a new binary decision variable I_{α} . Here, $I_{\alpha} = 1$ indicates that bus route α is selected as a BEB route. Once all directed links $(m, n) \in L$ are assigned to the H areas, we define L_A^h as the set of all links in the hth area. Consequently, we have the following relationship:

$$w_{h} = \frac{\sum_{\alpha \in \Omega_{\alpha}} \sum_{L:(m,n) \in L_{A}^{h} \cap L_{\alpha}} d_{mn} \cdot I_{\alpha}}{\sum_{L:(m,n) \in L_{A}^{h}} d_{mn}}, \forall h = 1, \dots, H.$$
(28)

Considering the bounded nature of Jain's index as defined in (27), we can observe that f(w) satisfies the inequality $1/H \le f(w) \le 1$. As the value of f(w) increases, the fairness level also increases, reaching maximum fairness when f(w) = 1 (100% fair). To ensure a desired fairness level, we introduce a constraint as follows:

$$f(w) = \frac{(\sum_{h=1}^{H} w_h)^2}{H \sum_{h=1}^{H} w_h^2} \ge \eta,$$
(29)

where η denotes a predetermined fairness level of the planning result, constrained to be between 1/H and 1.

This inequality constraint can be further rewritten as a second-order cone constraint:

$$\left\| \begin{array}{c} W_1 \\ \vdots \\ W_H \end{array} \right\|_2 \le \sum_{h=1}^H \sqrt{\frac{1}{H \cdot \eta}} w_h. \tag{30}$$

The introduction of I_{α} necessitates the reformulation of certain constraints in the section of Constraints. First, it enables us to quantify the initial energy $e_{\alpha,o_{\alpha}}$ saved in all BEB batteries as below:

$$e_{\alpha,o_{\alpha}} = \theta_0 \cdot u_{\alpha}^{bat} \cdot I_{\alpha}, \forall \alpha \in \Omega_{\alpha}.$$
(31)

In a similar fashion, we can redefine constraints (6)-(8) as follows:

$$e_{\alpha,m} \ge \theta^l \cdot u_{\alpha}^{bat} \cdot I_{\alpha}, \forall \alpha \in \Omega_{\alpha}, \forall m \in N^T,$$
(32)

$$e_{\alpha,m} + s_{\alpha,m} \le \theta^u \cdot u_\alpha^{bat} \cdot I_\alpha, \, \forall \alpha \in \Omega_\alpha, \forall m \in N^T,$$
(33)

$$e_{\alpha,n} = e_{\alpha,m} + s_{\alpha,m} - e^0 \cdot d_{mn} \cdot I_{\alpha}, \, \forall \alpha \in \Omega_{\alpha}, \, \forall (m,n) \in L_{\alpha}.$$
(34)

Regarding BEB routes, when $I_{\alpha} = 1$, constraints (32)-(34) are equivalent to (6)-(8). On the other hand, for non-BEB routes where $I_{\alpha} = 0$, we have $e_{\alpha,o_{\alpha}} = e_{\alpha,m} = s_{\alpha,m} = 0$.

Furthermore, additional constraints need to be incorporated to account for the new decision variable I_{α} , which ensures that buses can only charge if their routes are designated for BEBs:

$$y_{\alpha,m} \le I_{\alpha}, \forall \alpha \in \Omega_{\alpha}, \forall m \in N^T.$$
(35)

And if a bus on route α never undergoes charging, it indicates that the route is not intended for BEBs.

$$I_{\alpha} \leq \sum_{m \in N^{T}} y_{\alpha,m} , \forall \alpha \in \Omega_{\alpha}.$$
(36)

Considering the budget limitations associated with constructing on-route charging facilities, we impose an upper limit on the number of BEB routes:

$$\sum_{\alpha \in \Omega_{\alpha}} I_{\alpha} \le I_{\max},\tag{37}$$

where I_{max} represents the maximal number of BEB routes to be invested in the planning period. And we introduce the following binary constraint:

$$I_{\alpha} \in \{0,1\}, \, \forall \alpha \in \Omega_{\alpha}. \tag{38}$$

As a result, the model formulation that takes fairness measurement into consideration remains a MISOCP problem:

$$\min \sum_{m \in N^{T}} (f_{s,m} \cdot X_{m} + f_{c,m} \cdot \beta_{m}) + \sum_{m \in N^{T}} \sum_{i \in N^{G}} c_{i,m} \cdot \Psi_{i,m} + \sum_{\mathcal{E}:(i,j)} T \cdot c_{e} \cdot \ell_{ij} \cdot r_{ij}$$

$$\text{s.t.} (2) - (5), (9) - (11), (14) - (25), (28), (30) - (38).$$
(39)

6. Planning Results

6.1 Planning Results without Fairness

Assuming a 10-year planning period, we begin by solving the planning model (26) without incorporating any fairness constraints. Table 2 provides information on the frequency of on-route charging required to sustain the round trips for all 15 bus routes. The table illustrates that as the initial SOC of the BEB batteries increases, the overall number of required charging sessions decreases. Notably, once the initial SOC exceeds 50%, all BEBs are capable of completing their round trips without the need for on-route charging. This finding highlights the importance of ensuring that BEBs are charged to adequate SOC levels prior to departure, which can help optimize their operational efficiency and minimize the need for additional charging infrastructure.

	Round-trip	Charge Power	Initial SOC θ_0				
Route	Length (mile)	(kW)	0.1	0.2	0.3	0.4	>=0.5
22	13.82	150	1	0	0	0	0
101	28.28	200	3	2	0	0	0
102	47.81	200	5	4	2	1	0
111	52.34	200	5	4	3	1	0
150	44.18	200	5	3	2	0	0
153	16.37	150	2	1	0	0	0
156	25.04	150	2	1	0	0	0
168	24.35	150	2	1	0	0	0
177	48.66	200	5	4	2	1	0
181	30.08	150	2	1	0	0	0
182	15.10	150	1	0	0	0	0
183	21.79	150	2	1	0	0	0
187	11.81	150	1	0	0	0	0
190	41.79	200	4	3	2	0	0
193	50.62	200	5	4	2	1	0

Table 2 On-Route Charging Frequency per Round-Trip for Each BusRoute at Different Departure SOC

Table 3 presents the planning results for initial SOC values ranging from 0.1 to 0.4, considering that on-route charging is no longer needed for the 15 BEBs when their initial SOC reaches or exceeds 50%. The table demonstrates that increasing the initial SOC leads to a decrease in the total planning cost. This reduction can be attributed to the decreased charging demand resulting from a higher initial SOC, which in turn reduces the investment required for charging stations and piles. Additionally, the cost of power line investment decreases consistently as the length of power lines depends on the number of charging stations and the distance between the stations and the power nodes in which they are integrated. When $\theta_0 = 0.4$, the power line investment becomes zero because the three charging stations are built directly on the power nodes, eliminating the need for

extra power lines to connect the stations to the power grid. Moreover, the cost of power loss declines steadily with increasing θ_0 , reflecting the fact that BEBs with adequate SOC require less electric power, resulting in lower current flow in the power lines and reduced power loss.

When Initial SOC Ranges from 0.1 to 0.4						
Planning Metric	$\theta_0 = 0.1$	$\theta_0 = 0.2$	$\theta_0 = 0.3$	$\theta_0 = 0.4$		
Number of stations	27	14	7	3		
Number of piles	45	29	13	4		
Total cost	\$10,118,392	\$4,329,727	\$2,033,864	\$926,386		
Charging station investment	\$5,400,000	\$2,800,000	\$1,400,000	\$600,000		
Charging pile investment	\$1,125,000	\$725,000	\$325,000	\$100,000		
Power line investment	\$3,156,620	\$463,221	\$62,508	\$0		
Power loss cost	\$436,772	\$341,506	\$246,356	\$226,386		

 Table 3 Summary of Planning Results without Fairness Consideration

 When Initial SOC Ranges from 0.1 to 0.4



Figure 4 Optimal placement and charging pile allocation result of charging stations without fairness consideration.

Figure 4 displays the siting and sizing outcomes of on-route fast charging stations, represented by the transportation node ID and the number of charging piles installed at each station. Since each bus route has its dedicated charging piles, we can determine the number of bus routes being

charged at each station by counting the corresponding charging piles. When $\theta_0 = 0.1$, all origin stations of the 15 identified BEBs are included in these 27 charging stations. Notably, transportation node 83 situated in the Industrial District (SODO Busway & S Royal Brougham Way) hosts the highest number of BEB routes that charge here, totaling 4 routes. This node serves as an on-route bus stop for 5 BEB routes, which is consistent with selection rule 1) that designates common stops. Additionally, among the nodes with three charging piles, nodes 4 and 9 are origin stations for two bus routes each, while nodes 21 and 77 serve for no fewer than 3 bus routes.

When $\theta_0 = 0.2$, only one origin station for route 153, located at node 31, still requires the construction of charging stations. However, as θ_0 increases to 0.3 and 0.4, none of the origin stations require charging stations since the BEBs have enough energy to run the first few stops while maintaining a safe SOC. With a larger initial SOC, the number of charging stations decrease evidently which aligns with the findings in Table 3. From $\theta_0 = 0.2$ to 0.4, the number of BEB routes requiring on-route charging decreases. At $\theta_0 = 0.4$, only four routes require on-route charging, as confirmed by the data in Table 2. The nodes with the most charging piles built between $\theta_0 = 0.2$ and 0.4 are common stops, including nodes 54, 77, 83, and 10. This highlights the importance of building on-route charging stations at stops that serve multiple routes and further validates the effectiveness of selection rule 1) in forming the coupled network.

6.2 Planning Results with Fairness Consideration

In this section, we will maintain the assumption of a 10-year planning period. However, we will now incorporate the fairness measurement (30) into the planning model, as represented by (39). Notably, a maximum of 5 BEB routes $I_{max} = 5$), which is one-third of the total bus routes, will be selected for investment. To include all 15 bus routes as candidate BEB routes, we will set the initial SOC to 0.1 based on the information provided in Table 2. This approach will enable us to evaluate both the horizontal equity of the BEB route ratio across the population-based merged subareas and the vertical equity within the bus-commuter-based merged subareas.

a Maximum Number of BEB Routes $I_{\text{max}} = 5$						
Planning Metric	$\eta = 0$	$\eta = 0.9$	$\eta = 0.95$	$\eta = 0.99$		
Objective	\$2,002,226	\$2,002,226	\$2,166,931	\$2,879,586		
Number of stations	7	7	7	10		
Number of piles	8	8	8	11		
Station investment	\$1,400,000	\$1,400,000	\$1,400,000	\$2,000,000		
Pile investment	\$200,000	\$200,000	\$200,000	\$275,000		
Power line investment	\$142,253	\$142,253	\$307,758	\$340,780		
Power loss cost	\$259,973	\$259,973	\$259,173	\$263,806		
Fairness index	0.915800	0.915800	0.959993	0.992838		
BEB route ID	['182' '187' '168' '153' '22']	['182' '187' '168' '153' '22']	['187' '168' '183' '153' '22']	['182' '168' '153' '22' '190']		

Table 4 Summary of Planning Results Considering Horizontal Equity with a Maximum Number of BEB Routes $I_{max} = 5$

Table 4 presents the planning results of the horizontal equity analysis across four subareas merged based on the population feature. The fairness level η ranges from 0 to 0.99, with a value of 0 renderings (30) invalid. In such cases, the initial fairness index f(w) is computed, prioritizing the minimization of the total planning cost. As the value of η increases, a stricter rule is imposed on the equitable distribution of BEB routes among the four subareas. Figure 5 illustrates the allocation of these five BEB routes when $\eta = 0.99$, demonstrating a similar proportion of BEB routes to all bus routes in each subarea.



• Transportation node 🔵 Charging station — Original route — BEB route

Figure 5 Planning results reflecting the highest level of horizontal equity across 4 subareas.

Without considering (30), the initial fairness index achieved through the most cost-effective planning scheme is 0.915800, surpassing the fairness level of 0.9. Therefore, we observe that the planning results are identical for fairness levels of 0 and 0.9 in Table 4. However, as the fairness level increases to 0.95, we observe a corresponding rise in the planning cost, primarily due to increased power line investment expenses. This adjustment is necessary to ensure a higher level of fairness, leading to a reconsideration of the five BEB route IDs. Specifically, from fairness levels of 0.9 to 0.95, route 183 replaces route 182 as one of the BEB routes to be invested in.

At a fairness level of 0.99, the planning model requires three additional charging stations and three more charging piles to accommodate the replacement of routes 187 and 183 with routes 182 and 190 as BEB routes. This expansion of the charging infrastructure leads to increased costs in both power line investments and power loss. The planning model prioritizes fairness by selecting bus routes with higher on-route charging demand to be included as BEB routes, even if it results in higher planning costs. These findings underscore the inherent trade-off between equity and economic efficiency in the planning process. While striving for an equitable distribution of BEB routes, compromises need to be made in terms of increased economic expenses.

Similarly, we solve (39) again and present the planning results in Table 5. Notably, the planning metrics for $\eta = 0$ in Table 5 and Table 4 are nearly identical, with only slight variations in the calculated fairness index due to the utilization of different subareas. Within the bus-commuter-based merged subareas, the initial fairness index is 0.687317, which falls below the threshold of 0.9. Consequently, the planning outcomes for fairness levels of 0 and 0.9 are no longer the same.

Maximum Number of BEB Routes $I_{max} = 5$							
Planning Metric	$\eta = 0$	$\eta = 0.9$	$\eta = 0.95$	$\eta = 0.99$			
Objective	\$2,002,226	\$2,403,729	\$2,825,122	\$2,960,454			
Number of stations	7	8	8	11			
Number of piles	8	9	9	12			
Station investment	\$1,400,000	\$1,600,000	\$1,600,000	\$2,200,000			
Pile investment	\$200,000	\$225,000	\$225,000	\$300,000			
Power line investment	\$142,253	\$307,758	\$729,021	\$182,242			
Power loss cost	\$259,973	\$270,972	\$271,101	\$278,212			
Fairness index	0.687317	0.901361	0.986707	0.996923			
BEB route ID	['182' '187' '168' '153' '22']	['182' '187' '168' '183' '153']	['181' '182' '187' '183' '153']	['182' '187' '168' '177' '153']			

Table 5 Summary of Planning Results Considering Vertical Equity with a Maximum Number of BEB Routes $I_{max} = 5$

As the fairness level increases from 0 to 0.9, there is a corresponding increase in the planning cost, and an additional charging station is required when $\eta = 0.9$. This adjustment involves replacing route 22 with route 183. When η further increases to 0.95, the investment cost in charging infrastructure remains relatively stable, but there is a significant rise in power line investment. This change can be attributed to the altered locations of the charging stations. Interestingly, at $\eta = 0.99$, although three additional charging stations must be constructed, there is a reduction in the investment required for power lines. This is due to the decreased total distance between the charging stations and the power grid nodes. However, the increase in both power loss costs and investment in charging infrastructure outweighs the savings achieved, leading to the highest planning cost when $\eta = 0.99$.



• Transportation node (Charging station 🛛 — Original route 🚽 BEB route

Figure 6 Planning results reflecting the highest level of vertical equity across 3 subareas.

The distribution of the five BEB routes and the locations of their charging stations within the three bus-commuter-based merged subareas are visualized in Figure 6 for a fairness level of $\eta = 0.99$. Comparing this figure with Figure 5, we can observe that routes 22 and 190 from Figure 5 have been replaced by routes 187 and 177 in Figure 6. This adjustment from horizontal equity to vertical equity results in longer BEB routes (as indicated in Table 2) primarily located in the western portion of the census tracts.

This observation suggests that residents in the western region have a higher reliance on bus transportation, which aligns with the actual transportation landscape. In contrast, the eastern part of King County shows a scarcity of bus routes, indicating that residents in this area must rely on alternative transportation methods, such as household cars, to fulfill their commuting needs.

7. Conclusions and Policy Implications

A coupled power and transportation network framework is established for the planning of on-route charging infrastructure for BEBs. By integrating charging stations into both networks, we consider not only the investment cost of charging stations and charging piles but also additional investment in power lines and increased power loss costs in the power grid. These costs are minimized through the utilization of MISOCP. Additionally, we introduce fairness measurements into the planning results using Jain's index, which aligns well with the MISOCP model. This allows decision-makers to customize the level of fairness implemented during different phases of fleet electrification. All experiments in this study were conducted in South King County, a region recognized for being at the forefront of full electrification efforts. This area has been significantly impacted by air pollution, making it a pertinent location for our research.

Without fairness measurements, we compare the planning results under different levels of battery SOC when BEBs depart from origin stations. This analysis assists decision-makers in predicting the need for additional on-route charging infrastructure based on the current on-base charging station condition. Our siting and sizing results indicate that, regardless of the initial SOC of BEB batteries, on-route charging stations are more likely to be located at stops serving multiple routes.

Furthermore, we incorporate a fairness measurement by imposing the fairness constraint in the planning model. By merging census tracts that intersect with bus routes into distinct subareas based on two tract features - the resident population and the population of bus commuters - we are able to measure both horizontal and vertical equity in the planning results. Comparing the planning outcomes under different fairness levels, we observe that a greater emphasis on fairness in the distribution of BEB routes among subareas results in higher planning costs. This information offers valuable insights to decision-makers on how to strike a balance between equity and economic efficiency in fleet electrification planning.

Our framework, which leverages the existing bus route map to create a virtual power network, has the potential to be applied to transportation systems in other cities. Additionally, our MISOCP model and fairness measurements provide practical guidance for allocating budgets and promoting social justice during the step-by-step electrification of bus fleets. In future research, we aim to extend the application of this planning model to larger transit systems and investigate acceleration algorithms to enhance its computational efficiency.

REFERENCES

- United States Environment Protection Agency. Sources of greenhouse gas emissions, August 2022. URL <u>https://www.epa.gov/ghgemissions/sources-greenhouse-gasemissions</u>.
- [2] Jakov Topić, Jure Soldo, Filip Maletić, Branimir Škugor, and Joško Deur. Virtual simulation of electric bus fleets for city bus transport electrification planning. Energies, 13(13):3410, 2020.
- [3] Inside China's Electric Bus Capital. Bloomberg.com, May 2018. URL https://www.bloomberg.com/news/articles/2018-05-08/in-china-shenzhen-electrified-its-entire-bus-fleet.
- [4] Netherlands leads the way on new electric buses analysis, January 2022. URL <u>https://www.transportenvironment.org/discover/netherlands-leads-the-way-on-new-electric-buses-analysis/</u>.
- [5] Zero-emissions fleet King County Metro King County. URL https://kingcounty.gov/depts/transportation/metro/programs-projects/innovationtechnology/zero-emission-fleet.aspx.
- [6] Shyam SG Perumal, Richard M Lusby, and Jesper Larsen. Electric bus planning & scheduling: A review of related problems and methodologies. European Journal of Operational Research, 301(2):395–413, 2022.
- [7] Yusheng Wang, Yongxi Huang, Jiuping Xu, and Nicole Barclay. Optimal recharging scheduling for urban electric buses: A case study in davis. Transportation Research Part E: Logistics and Transportation Review, 100:115–132, 2017.
- [8] Meng Li, Peng Tang, Xi Lin, and Fang He. Multistage planning of electric transit charging facilities under build-operate-transfer model. Transportation Research Part D: Transport and Environment, 102:103118, 2022.
- [9] Yuping Lin, Kai Zhang, Zuo-Jun Max Shen, Bin Ye, and Lixin Miao. Multistage largescale charging station planning for electric buses considering transportation network and power grid. Transportation Research Part C: Emerging Technologies, 107:423–443, 2019.
- [10] Matthias Rogge, Evelien Van der Hurk, Allan Larsen, and Dirk Uwe Sauer. Electric bus fleet size and mix problem with optimization of charging infrastructure. Applied Energy, 211:282–295, 2018.
- [11] Jinwoo Lee, Heeseung Shon, Ilia Papakonstantinou, and Sanghoon Son. Optimal fleet, battery, and charging infrastructure planning for reliable electric bus operations. Transportation Research Part D: Transport and Environment, 100:103066, 2021.
- [12] Dan McCabe and Xuegang Jeff Ban. Optimal locations and sizes of layover charging stations for electric buses. Transportation Research Part C: Emerging Technologies, 152:104157, 2023.
- [13] King County Metro Transit. King county metro transit interim base implementation report, January 2020. URL <u>https://kingcounty.gov/~/media/depts/metro/programs-projects/zero-emissions-fleet/battery-electric-bus-implementation-report.pdf</u>.
- [14] Yi He, Ziqi Song, and Zhaocai Liu. Fast-charging station deployment for battery electric bus systems considering electricity demand charges. Sustainable Cities and Society, 48:101530, 2019.

- [15] Maria Xylia, Sylvain Leduc, Piera Patrizio, Florian Kraxner, and Semida Silveira. Locating charging infrastructure for electric buses in stockholm. Transportation Research Part C: Emerging Technologies, 78:183–200, 2017.
- [16] Onur Elma and Hossam A Gabber. Flywheel-based ultra-fast on-route charging system for public e-buses. In 2020 International Conference on Electrical, Communication, and Computer Engineering(ICECCE), pages 1–4. IEEE, 2020.
- [17] Zhaocai Liu, Ziqi Song, and Yi He. Economic analysis of on-route fast charging for battery electric buses: Case study in utah. Transportation Research Record, 2673(5):119–130, 2019.
- [18] Fang He, Di Wu, Yafeng Yin, and Yongpei Guan. Optimal deployment of public charging stations for plug-in hybrid electric vehicles. Transportation Research Part B: Methodological, 47:87–101, 2013.
- [19] Fang He, Yafeng Yin, Jianhui Wang, and Yanni Yang. Sustainability si: optimal prices of electricity at public charging stations for plug-in electric vehicles. Networks and Spatial Economics, 16:131–154, 2016.
- [20] Lixun He, Jun He, Liwen Zhu, Wentao Huang, Yanyang Wang, and Hua Yu. Comprehensive evaluation of electric vehicle charging network under the coupling of traffic network and power grid. Plosone, 17(9):e0275231, 2022.
- [21] Fang He, Yafeng Yin, and Jing Zhou. Integrated pricing of roads and electricity enabled by wireless power transfer. Transportation Research Part C: Emerging Technologies, 34:1–15, 2013.
- [22] Guibin Wang, Zhao Xu, Fushuan Wen, and Kit Po Wong. Traffic-constrained multiobjective planning of electric-vehicle charging stations. IEEE Transactions on Power Delivery, 28(4):2363–2372, 2013.
- [23] Hongcai Zhang, Scott J Moura, Zechun Hu, and Yonghua Song. Pev fast-charging station siting and sizing on coupled transportation and power networks. IEEE Transactions on Smart Grid, 9(4):2595–2605, 2018.
- [24] Raymond A. Mohl. Stop the Road: Freeway Revolts in American Cities. Journal of Urban History, 30(5):674–706, July 2004. ISSN 0096-1442. doi: 10.1177/0096144204265180. URL https://doi.org/10.1177/0096144204265180. Publisher: SAGE Publications Inc.
- [25] Christoffel Venter, Gail Jennings, Darío Hidalgo, and Andrés Felipe Valderrama Pineda. The equity impacts of bus rapid transit: A review of the evidence and implications for sustainable transport. International Journal of Sustainable Transportation, 12(2):140–152, February 2018. ISSN 1556-8318. doi: 10.1080/15568318.2017.1340528. URL https://doi.org/10.1080/15568318.2017.1340528. Publisher: Taylor & Francis _eprint: https://doi.org/10.1080/15568318.2017.1340528.
- [26] Alireza Ermagun, Fatemeh Janatabadi, and Sanju Maharjan. Inequity analysis of spatial mismatch for low-income socially vulnerable populations across america. Transportation research part D: transport and environment, 118:103692, 2023.
- [27] King County Metro Transit. King County Metro Transit Zero-Emission Bus Fleet Transition Plan, May 2022. URL https://kingcounty.gov/~/media/depts/metro/accountability/reports/2022/zero-emissionbus-fleet-transition-plan-may-2022.
- [28] King County Metro Transit. Feasibility of achieving a carbon-neutral or zeroemission fleet, March 2017. URL

https://kingcounty.gov/~/media/elected/executive/constantine/news/documents/Zero_Emi ssion_Fleet.pdf.

- [29] Todd M Litman. Evaluating transportation equity: Guidance for incorporating distributional impacts in transport planning. ITE journal, 92(4):43–49, 2022. ISSN 0162-8178.
- [30] Alexa Delbosc and Graham Currie. The spatial context of transport disadvantage, social exclusion and well-being. Journal of Transport Geography, 19(6):1130–1137, November 2011. ISSN 0966-6923. doi: 10.1016/j.jtrangeo.2011.04.005. URL https://www.sciencedirect.com/science/article/pii/S0966692311000469.
- [31] Rosalia Camporeale, Leonardo Caggiani, Achlle Fonzone, and Michele Ottomanelli. Quantifying the impacts of horizontal and vertical equity in transit route planning. Transportation Planning and Technology, 40(1):28–44, 2017.
- [32] Wei Fan and Randy B Machemehl. Bi-level optimization model for public transportation network redesign problem: Accounting for equity issues. Transportation Research Record, 2263(1):151–162, 2011.
- [33] Yirong Zhou, Xiaoyue Cathy Liu, Ran Wei, and Aaron Golub. Bi-objective optimization for battery electric bus deployment considering cost and environmental equity. IEEE Transactions on Intelligent Transportation Systems, 22(4):2487–2497, 2020.
- [34] Nahid Rezaeinia, Julio César Góez, and Mario Guajardo. Efficiency and fairness criteria in the assignment of students to projects. Annals of Operations Research, 319(2):1717–1735, 2022.
- [35] Neil Quarles, Kara M Kockelman, and Moataz Mohamed. Costs and benefits of electrifying and automating bus transit fleets. Sustainability, 12(10):3977, 2020.
- [36] Zhaocai Liu, Ziqi Song, and Yi He. Planning of fast-charging stations for a battery electric bus system under energy consumption uncertainty. Transportation Research Record, 2672(8):96–107, 2018.
- [37] Masoud Farivar and Steven H Low. Branch flow model: Relaxations and convexification—part i. IEEE Transactions on Power Systems, 28(3):2554–2564, 2013.
- [38] Rajendra K Jain, Dah-Ming W Chiu, William R Hawe, et al. A quantitative measure of fairness and discrimination. Eastern Research Laboratory, Digital Equipment Corporation, Hudson, MA, 21, 1984.
- [39] King County Metro Transit. metro.kingcounty.gov /GTFS/. URL https://metro.kingcounty.gov/GTFS/.
- [40] Robert Clay Prim. Shortest connection networks and some generalizations. The Bell System Technical Journal, 36(6):1389–1401, 1957.
- [41] Joseph B Kruskal. On the shortest spanning subtree of a graph and the traveling salesman problem. Proceedings of the American Mathematical society, 7(1):48–50, 1956.
- [42] Xinyi Zhao. GTFS_transpowernet: A specialized tool designed for electric bus planners. URL https://github.com/Xinyi-0724/GTFS_TransPowerNet/tree/main.
- [43] Xinyi Zhao. King County 24-node virtual power grid, March 2023. URL https://github.com/Xinyi-0724/KingCounty_24_node_virtual_power_grid. original-date: 2023-03-31T04:25:16Z.
- [44] National Renewable Energy Laboratory. King County Metro Battery Electric Bus Demonstration—Preliminary Project Results. Technical report, U.S. Department of Transportation, 2017.

- [45] Bus Testing and Research Center. Federal transit bus test: BYD Motors Inc. ELECTRIC BUS. Technical report, The Thomas D. Larson Pennsylvania Transportation Institute, June 2014. URL https://www.altoonabustest.psu.edu/busdetails.aspx?BN=1905.
- [46] Bus Testing and Research Center. Federal transit bus test: BYD Motors Inc. Model K11M. Technical report, The Thomas D. Larson Pennsylvania Transportation Institute, January 2020. URL https://www.altoonabustest.psu.edu/busdetails.aspx?BN=1307.
- [47] BYD Auto Co., Ltd. Bus: K9M BYD USA, . URL https://en.byd.com/bus/k9m/.
- [48] BYD Auto Co., Ltd. Bus: K11M BYD USA, . URL
- https://en.byd.com/bus/k11m/.
- [49] Gurobi Optimization, LLC. Gurobi Optimizer Reference Manual, 2023. URL https://www.gurobi.com.
- [50] US Census Bureau. Glossary, April 2022. URL <u>https://www.census.gov/programs-surveys/geography/about/glossary.html</u>. Section: Government.
- [51] Yang Ju, Lara J Cushing, and Rachel Morello-Frosch. An equity analysis of clean vehicle rebate programs in california. Climatic Change, 162:2087–2105, 2020.
- [52] Nicholas N Ferenchak and Wesley E Marshall. Equity analysis of proactively-vs. reactively-identified traffic safety issues. Transportation research record, 2673(7):596–606, 2019.
- [53] King County Metro. Consolidated Demographics Index for King County Census Tracts / demographic index area, March 2014. URL https://hub.arcgis.com/datasets/kingcounty::consolidated-demographics-index-for-kingcounty-census-tracts-demographic-index-area/about.
- [54] King County. Consolidated demographics index for king county census tracts | demographic index area, March 2014. URL https://hub.arcgis.com/maps/kingcounty::consolidated-demographics-index-for-kingcounty-census-tracts-demographic-index-area/about.
- [55] King County. ACS: Means Of Transportation To Work / acs b08301 transportation | King County GIS Open Data, February 2018.